



# Outline

In the EPSRC network “Maths Foresees”, the Environment Agency (EA) posed and stated two challenges:

- ▶ I. How can we **visualise return periods** of extreme (flooding) events to a general audience in a fluid-dynamical set-up?  
As opposed to ....
- ▶ This challenge is posed because people (often) mistakenly think that the time between extreme events of a certain magnitude expressed by a return period is (more or less) fixed, e.g. “I am safe for  $\sim 100$  years after a 1 : 100 year flood”. (BBC interview 2019 ....)
- ▶ *Answer to challenge-I*: the visualisation of return periods in the **Wetropolis flood investigator** (B. et al. (2020, 2024)).

## Outline-continued

In the EPSRC network “Maths Foresees”, the Environment Agency posed and stated two challenges:

- ▶ ...
- ▶ **II.** To apply mathematics to flood mitigation with tools that are comprehensible to decision-makers. As opposed to ...
- ▶ *Answer to challenge-II:* a **graphical cost-effectiveness tool** to visualise flood-mitigation scenarios.



## (Challenge-I) The weather machine: ingredients

The basic ideas and ingredients are the following:

- ▶ There is a **conceptual river catchment** with a river, a (one-sided) floodplain, a porous moor, a reservoir and downstream a city.
- ▶ Instead of 1:100 year extreme events in a 1000km<sup>2</sup> river catchment, say, **time and spatial scales need to be reduced**.
- ▶ There are only Wetropolis days ( $w_d$ ) of length  $T_d$ .
- ▶ It **rains in two locations**, in the moor and/or reservoir, or not: so there are 4 choices.
- ▶ It **rains** ( $f_1, f_2, f_3, f_4$ )  $T_d$  of a day with fractions  $0 < f_1 < f_2 < f_3 < f_4 < 1$ : so there are  $\geq 4$  “daily” rain amounts possible.
- ▶ If  $f_1 = 0.1$  then the rain rate during a day is a “unit”  $r_0$ .
- ▶ The river length  $L_r$  at slope 1 : 100 is  $L_r \in [1, 5]\text{m (-)}$ .
- ▶ Remaining design unknowns are therefore the **day length and “unit” rainfall rate**  $T_d, r_0$ .











## The weather machine: discussion

*Question:* Is it unusual for a mathematician to build or propose fluid-dynamical devices and demonstrations? 몰라요:

- ▶ The inventor of the Galton board “**Sir Francis Galton** was a British poly-math ...” (and mathematician).
- ▶ The **innovation of Wetropolis** lies in the coupling between the weather or rain machine with its skew-Galton boards and the conceptual river catchment.
- ▶ Underlying Wetropolis is a mathematical and numerical **design model** of PDEs, ODEs and diagnostic relations linking the equations for various components.
- ▶ Wetropolis is one member in a suite of fluid-dynamical demonstrations created with designer **Wout Zweers**.



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- Maths fights floods: <https://obokhove.github.io/UKsuccessFEVpreprint23102023.pdf> & <https://doi.org/10.1017/wat.2024.4>





## Video of Wetropolis-II: visualising extreme events

*Goal:* visualising return period/Annual Exceedance Probability  
(request EA & JBA Trust). <https://www.youtube.com/watch?v=yUjYfg2SfY0>



## Wetropolis: few remarks

- ▶ Rainfall in Wetropolis is **spatio-temporal**, so the occurrence/distribution of flooding events is more complicated than the imposed random rainfall distribution. TBD.
- ▶ **Climate change** has been implemented via a switch activating rainfall in an additional upstream extra lake/reservoir that is in sync with the random rainfall in the moor. It adds on average  $\sim 20\%$  more rain to Wetropolis.
- ▶ A Galton board yields a normal distribution in the infinite-row limit. What skew-Galton-board specification would lead to other (known) skew- or **extreme-value probability distributions**?
- ▶ By using an **LED-board with visualised “Galton-board” channels** various computer-generated discrete distributions can be implemented (Robin Furze).











## How (well) can we mitigate flooding?

Giving-room-to-the-river – GRR, extra channel in River Waal/Rhine Nijmegen (NL):



# How (well) can we mitigate flooding?

Flood-plain storage –FPS & dynamic weir control:



## How (well) can we mitigate flooding?

Extra storage –FPS active flooding of certain areas (Merwede, Storm Ciara, NL,  $20\text{Mm}^3$ ):



# How (well) can we mitigate flooding?

Natural <sub>flood</sub> management – N<sub>FM</sub> 1300 leaky dams & trees (public engagement & co-benefits, e.g. carbon sequestration)



Central part of one of the two experimental timber bunds in the River Seven catchment

# How (well) can we mitigate flooding?

Imagine your home is flooded. Lots of **beaver colonies** then? Extra water storage behind dams:  $\sim 1100\text{m}^3 = 1.1\text{Mlitres}$  (or  $1/5^{\text{th}}$ ).

## How beavers can help stop homes from flooding

© 17 Feb 2020 Last updated at 11:08

**not**



**Beavers** can play an important role in helping to keep our homes from being flooded.

That's according to scientists at Exeter University, who have carried out a five year study of wild animals living in Devon.

They found the animals helped to [redacted] reduce pollution and boost wildlife population.

# How (well) can we mitigate flooding?

SuDS –Sustainable Drainage Systems:



# How (well) can we mitigate flooding?

Dredging –Wainfleet Flood Action Group (flood June 2019, 67 homes & lots of farmland flooded):



# How (well) can we mitigate flooding?

Resilience: raising of new houses now mandatory in Wainfleet:

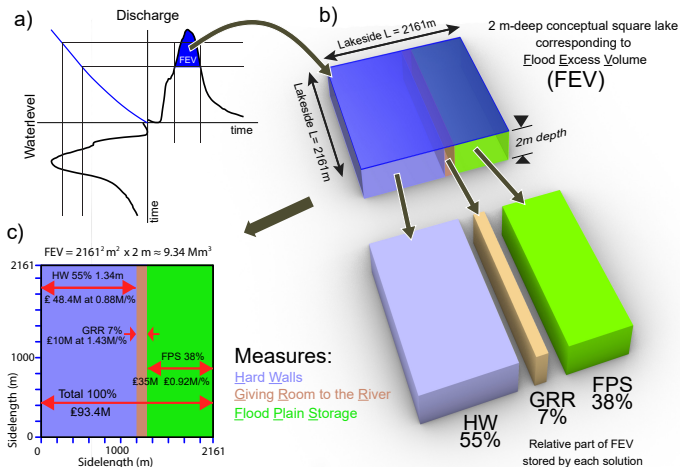


# How (well) can we mitigate flooding?

Resilience: responsible flood-plain development (**zero-sum or negative volume rule**), Rhine valley:



# Graphical cost-effectiveness tool for flood mitigation



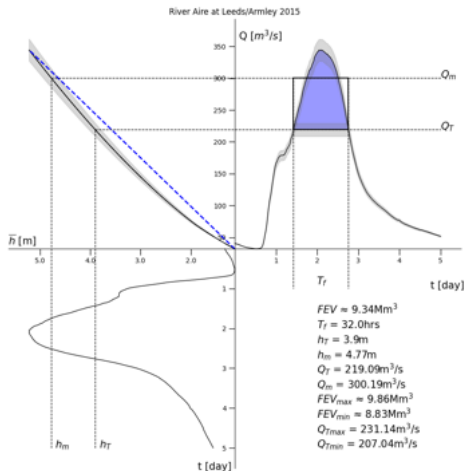
# Graphical cost-effectiveness tool: three-panel graphs

Motivated by Boxing Day  
2015 floods:

*Flood-excess volume (FEV)* is defined as volume of flood water one wishes to mitigate (i.e., reduce to zero) by cumulative effect of flood-mitigation measures.

Right:

River Aire gauge data of Jan. 2015 floods. **Bottom left:** 15min water-stage time series. **Top left:** longer-time rating curve. **Top right:** resulting discharge time series.



## Graphical cost-effectiveness tool: square lake (1 : 200yr design flood)

B et al. 2020 *Water*:

Scenario S1 (of 4) in a square-lake cost-effectiveness analysis of flood-alleviation plans using flood-excess volume (FEV); each mitigation measure is represented by a colour, and an overall cost analysis is displayed.

**HW:** higher walls,

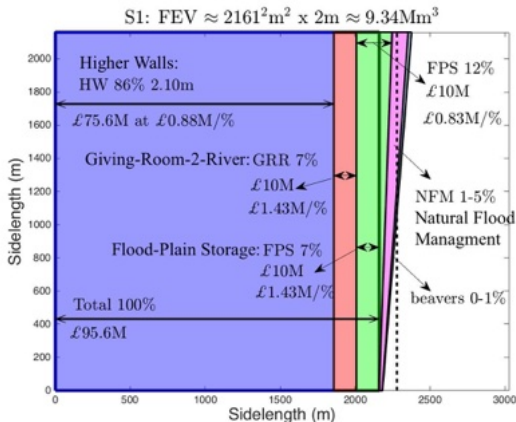
**GRR:**

giving-room-to-the-river,

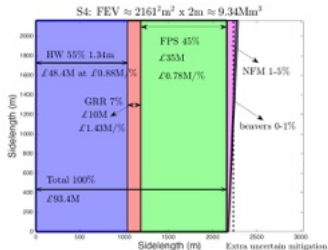
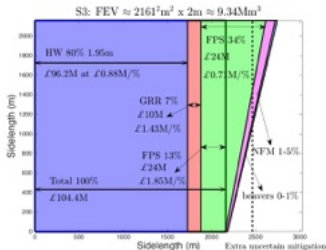
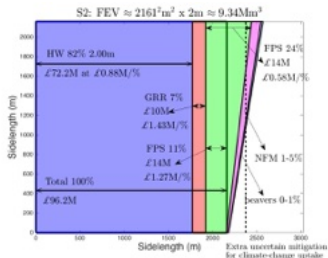
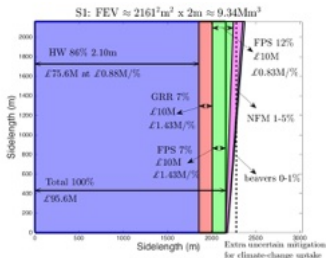
**FPS:** flood plain storage,

**NFM:** Natural flood management,

**beavers:** 85 beaver colonies.



## Graphical cost-effectiveness tool: square lake scenarios (1 : 200yr design flood)



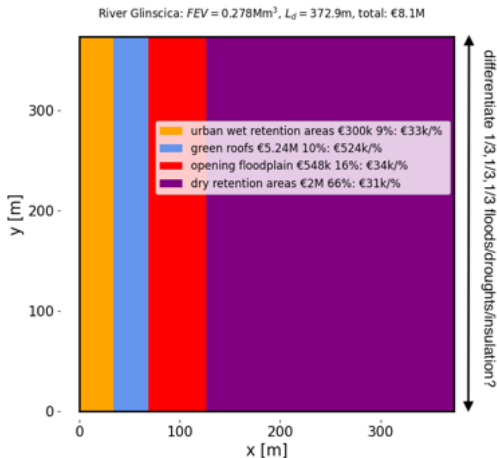
# A priori FEV analysis: NBS for River Glinščica (1:100yrs)

Pengal et al. 2021 (EU project NAIAD):

A demonstration of **participatory catchment management with stakeholders** was undertaken for NBS as most suitable solution to reach these primary goals.

## 4 Nature Based Solutions (NBS) considered:

urban wet retention areas 9%  
green roofs (floods/ droughts/ insulation) 10%  
opening of flood plains 16%  
dry retention areas 66%  
with round-off.

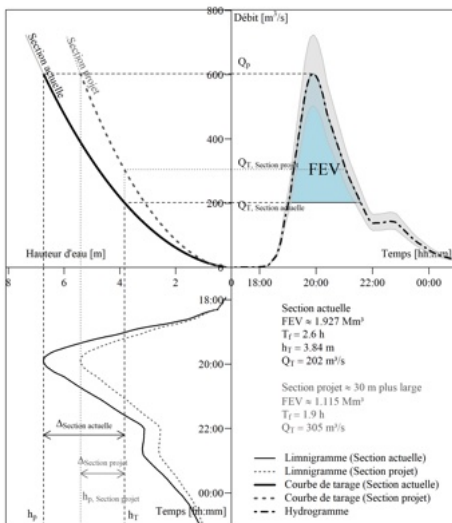


# A posteriori FEV analysis: River Brague, France (1:500yrs)

Piton & Tacnet 2020  
(NAIAD) after River Brague:

Based on data of hydrographs  
across the catchment  
following hydraulic  
simulations, FEV was  
calculated.

Three-panel graph of the 2015  
flood of the River Brague,  
France, solid-line curves, as  
well as a **GRR-modified case**,  
dashed curves.

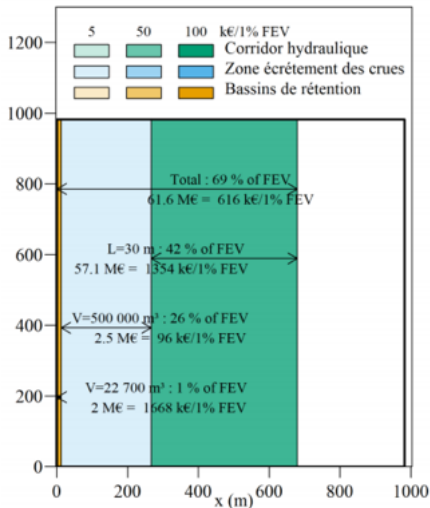


# A posteriori FEV analysis: River Brague (1:500yrs)

Piton & Tacnet 2020:

Three measures cover 69% of the FEV: with **concrete basins** at 1% represented by the thin sliver, **natural retention areas** at 26% being the cheapest **per percent** and **GRR** at 42%.

Remaining 31% **unprotected FEV** requires additional measures for the worst-case design event of 1:500yrs or  $AEP = 0.2\%$ .



# Graphical tool and its ability to find inconsistencies

FEV and square-lake analysis-tool **uncovered inconsistencies** in a public [REDACTED] report (B et al. 2018, 2020):

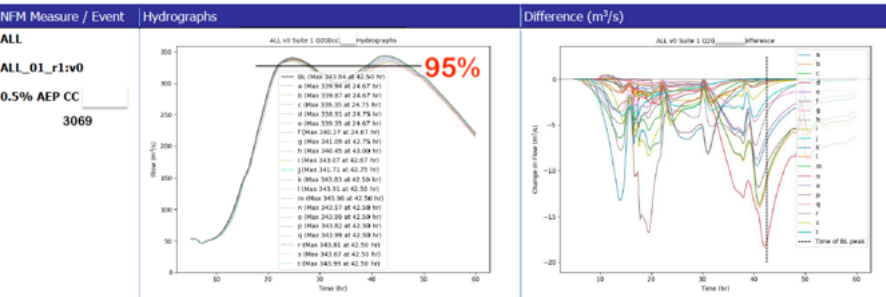
- ▶ Analysis showed that efficacy of Natural Flood Management (NFM) low [1, 5]% and has been (grossly) overstated;
- ▶ two vastly different flood-plain storage volumes emerge from this report leading us to define the novel concept of *available flood-storage volume*; and,
- ▶ the locations of weirs for the proposed dynamic flood-plain storage are suboptimal.



# Graphical tool and its ability to find errors (02/07-2024)

FEV and square-lake analysis-tool uncovered (apparent) **errors** in private-public plans:

- ▶ A [REDACTED] Company's (RC) claim of 5% flood reduction by NFM against Climate Change effects is seemingly not seen in graphs provided as evidence, e.g., [11-06-2025: graphs in Calverley, control upstream weir and show graphs in Leeds?]:



# Graphical tool and its ability to find errors (02/07-2024)

FEV and square-lake analysis-tool uncovered (apparent) errors in private-public plans:

- ▶ Response (lukewarm) by [REDACTED]:  
“ [REDACTED] ”
- ▶ To date 20-09-2024: data sharing of relevant hydrographs has been refused by [REDACTED] and “*limited time for a peer review*” .
- ▶ Are the (potential) investors in the flood works proposed (£4.25M needed) by RC aware of this anomaly between the claimed 5% efficacy and the (hitherto apparent lack of) evidence? Evidence provided seems to show only  $\sim 1.5\%$ ?
- ▶ The missing  $\sim 1.5\%$  was stated to come from landmanagement including soil aeration (**which is not NFM**) but corresponding evidence has hitherto been lacking.

# Graphical tool and its ability to find errors: remarks

Morgan and Henrion's advice (§7.8 "Uncertainty: ...", 1990) seems to apply:

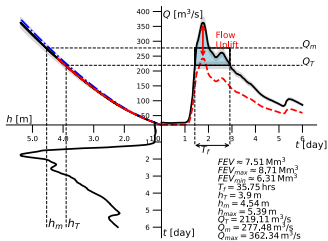
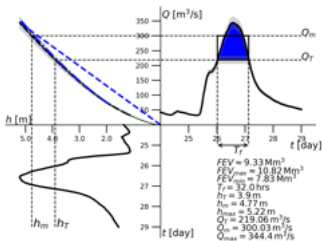
- ▶ *"This means, however, that **peer review** should be more uniformly extended to policy focussed research and analysis than it has been in the past"*.
- ▶ *"... to develop institutions and traditions that **protect experts who participate in elicitation from subsequent legal or other entanglements**. ... has set an excellent example by providing partial anonymity to participating experts"*.
- ▶ Note that this **anonymity is in apparent conflict** with the UK academic and REF demands with associated funding to demonstrate impact.
- ▶ The central issue seems to be that **scrutiny of public/private spending**, here on flood-mitigation, by academics and especially by mathematicians, **is uncommon**.
- ▶ Since 07-2024, I have further flagged the (potential) issue with the EA and contractors of the RC for further (informal) investigation.
- ▶ Such a reluctance to scrutiny should be a point in a wider discussion.

# Graphical tool and its ability to find errors: remarks

Manuscript by Natasha Pullan (winner King Prize 24/25 SoM-UoL) & OB (2026)  
reveals novel & disturbing findings:

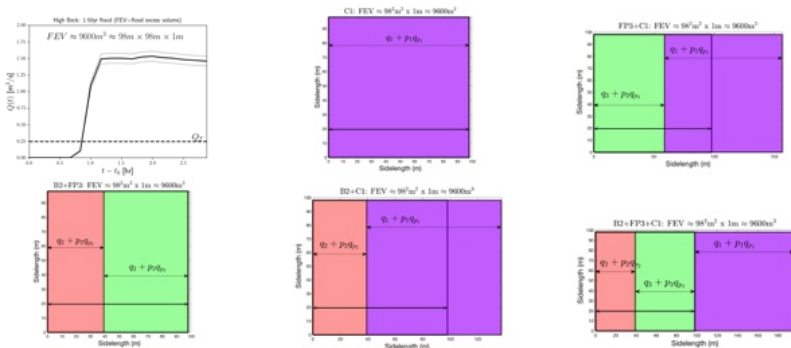
- ▶ 2020 minor flood of River Aire in Leeds can become major 2015 flood in 2100 when projected 51% climate-change uplift is applied.
- ▶ Example of storyline approach to climate change –see nonfiction story in Appendix <https://eartharxiv.org/repository/view/13645/>
- ▶ The major 2015 flood uplifted by 51% in 2100 would become a disaster: cost-effectiveness tool applied reveals Leeds unprepared.
- ▶ The choice of flood ensembles for flood-mitigation analysis is very important: deliberately using biased ensembles incorrectly increases efficacy of NBS/NFM (see examples in manuscript). This is misleading & can lead to poor decisions on flood-mitigation funding.

# Storylining of climate-change uplift



# High Beck flood-mitigation case study (1:10yrs)

- Square-lake plots: **size** & **costs** with flood-excess volume & mitigation measures.
- Base costs  $q_i$ , probability failure  $p_i$ , repair costs  $q_{p_i}$ ,  $i = 1, 2, 3$ ; **costs**  $q_i + p_i q_{p_i}$ .
- Combine Canal C1, bund B2, flood-plain-storage FP3 into 5 scenarios:



- **Utility functions:**  $U_{23} = \sum_{j=1}^5 w_j C_j$ ,  $U_1 = \sum_{j=1}^5 (w_j C_j - \sum_{k=1}^{N_j} \alpha_{kj} B_{jk})$   
 (co-benefits  $B_{jk}$ : e.g., droughts, extra CC, less pollution); if  $B_{jk} = 0$ :  $U_1 > U_{23}$ .
- If  $B_{jk}$  **unknown**,  $U_1 = U_{23}$ : appreciating benefits w. **info-gap theory**, [B. 2025](#).

# Discussion on visualising cost-effectiveness of flood mitigation

- ▶ FEV-analysis seemingly 0D but it captures a stretch of river, so becomes 1D.
- ▶ A priori investigation can be extended by using **ensemble forecasts** leading to an FEV cost-effectiveness analysis with **uncertainty**: see B et al. 2020 *Water* for a detailed roadmap.
- ▶ In-depth **Socratic-style dialogue** on critique, see B 2021 *ESREL2021*.
- ▶ In summary, the **FEV cost-effectiveness approach is an essential input in the whole chain**.
- ▶ It provides **valuable inputs in global approaches** dedicated to multifactorial analysis of flood protection measures' effectiveness.
- ▶ Note that our FEV tool is **by itself and alone not a proper safety** and reliability analysis approach.
- ▶ However, it is **an essential input in the whole chain**.

## Wetropolis World: future work

How can a **Wetropolis laboratory set-up** and a “**Numerical Wetropolis Prediction**” model be used to understand:

- ▶ risk, extreme weather & flooding probability statistics –revisit **spatial-temporal rainfall** & change-point analysis;
- ▶ flood control –e.g., reservoirs in Wetropolis;
- ▶ data assimilation & parameter estimation –laboratory experiment as “**truth run**”?
- ▶ One Wetropolis World’s **goal**: to investigate “classical” PDE & Data Assimilation “**NWP**” model with ML predictions.

